

Renormalization of hole-hole interaction at decreasing Drude conductivity

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The diffusion contribution of the hole-hole interaction to the conductivity is analyzed in gated GaAs/In_xGa_{1-x}As/GaAs heterostructures. We show that the change of the interaction correction to the conductivity with the decreasing Drude conductivity results both from the compensation of the singlet and triplet channels and from the arising prefactor $\alpha_i < 1$ in the conventional expression for the interaction correction.

The quantum corrections to the conductivity in disordered metals and doped semiconductors are intensively studied since 1980.¹ Two mechanisms lead to these corrections: (i) the interference of the electron waves propagating in opposite directions along closed paths (WL correction); (ii) electron-electron ($e-e$) or hole-hole ($h-h$) interaction.

The role of the $e-e$ ($h-h$) interaction has been a subject of theoretical^{1,2,3,4,5,6,7,8,9} and experimental^{10,11,12} studies for more than two decades. The new interest in the matter is associated with discussion of the nature of metallic-like temperature dependence of the conductivity observed at low temperature in some two dimensional (2D) systems, e.g., in n-Si MOSFET and in dilute 2D hole gas in Al_xGa_{1-x}As/GaAs and Ge_{1-x}Si_x/Ge structures (see Refs. 13,14,15 and references therein). As a rule such behavior is observed in low-density high-mobility structures with the relatively large value of the gas parameter $r_s = \sqrt{2}/(a_B k_F)$ characterizing the interaction strength and by too high value of $T\tau$ (hereafter we set $\hbar = 1$, $k_B = 1$), where a_B , k_F , and τ are the Bohr radius, the Fermi quasimomentum, and the transport relaxation time, respectively. The role of the interaction at $r_s > 3 - 5$ (i.e., at strong interaction), and/or $T\tau \gtrsim 1$ (i.e., at intermediate and ballistic regimes) was theoretically studied in Refs. 2,4,5,16,17,18,19,20, the experimental situation was reviewed in Refs. 13,14,15.

It should be noted that the metallic-like behavior is observed when the conductivity is not too high, therefore the corrections can lead to essential change of the conductivity with the temperature. The changing of the interaction correction at decreasing temperature and/or conductivity was theoretically studied in framework of the theory of the renormalization group (RG) in the papers.^{3,6,7,8,16,17} It has been shown that the correction renormalization depends on both the Drude conductivity and the Fermi liquid amplitude γ_2 that controls the $e-e$ interaction in the triplet channel. The contributions from singlet and triplet channels are opposite in sign favoring localization and antilocalization, respectively. In conventional conductors with high values of the Drude conductivity, $\sigma_0 = \pi k_F l G_0 \gg G_0$ [where l is the mean free path and $G_0 = e^2/(2\pi^2 \hbar)$], the initial value of the amplitude γ_2 is small, and the net effect is in favor of

localization. At $\sigma_0 \lesssim (10 - 15)G_0$ or in dilute systems, however, this amplitude may be enhanced due to $e-e$ correlations and thus results in metallic sign of $d\sigma/dT$.^{16,17}

Significantly less is known about the role of the interaction correction in disordered 2D systems when the $k_F l$ value tends to unity, i.e., at crossover from weak to strong localization. Experimentally, this effect was studied in the simplest single-valley electron 2D system GaAs/In_{1-x}Ga_xAs/GaAs with small g factor.²¹ It was shown that the net value of the interaction correction decreases rapidly with the σ_0 decrease at $\sigma_0 \lesssim (12 - 15)G_0$ ($k_F l \lesssim 4 - 5$). Such a behavior can result from the compensation of the contributions of the singlet and triplet channels as well as from suppression of both contributions with decreasing σ_0 . It is impossible to separate these two effects in the systems with small value of the g factor. The situation changes drastically when dealing with a system with large enough g factor. In this case the magnetic field can be used as a tool allowing to control the ratio between the two different contributions because it strongly suppresses the triplet channel and leaves the singlet channel unchanged. As shown below the hole 2D gas in strained GaAs/In_xGa_{1-x}As/GaAs structures is a suitable object to study the renormalization of the interaction quantum correction with the conductivity decrease. In a previous paper, Ref. 22, we have studied these structures at high Drude conductivity, $\sigma_0 > 30G_0$.

In this paper we report the results of experimental study of the evolution of the interaction correction to the conductivity in a p -type 2D system with decreasing Drude conductivity within the range from $\simeq 30G_0$ to $\simeq 3G_0$ when the ballistic contribution of the $h-h$ interaction is small. Firstly, we will outline the procedures used for extracting the diffusion part of the interaction correction and the value of the Fermi liquid parameter $F_0^\sigma = -\gamma_2/(1 + \gamma_2)$ from the dependences of ρ_{xx} and ρ_{xy} on the temperature and magnetic field. Then, we will discuss the change of F_0^σ with decreasing Drude conductivity. Finally, we will show that the reduction of the interaction correction with the decreasing Drude conductivity results from both the compensation of the singlet and triplet channels and from the arising of a prefactor $\alpha_i < 1$ in the conventional expression for the interaction correction.²

I. EXPERIMENT

We have measured the temperature and magnetic field dependences of ρ_{xx} and ρ_{xy} in the heterostructures GaAs/In_xGa_{1-x}As/GaAs grown by metal-organic vapor phase epitaxy on semiinsulating GaAs substrate. The lattice mismatch between In_xGa_{1-x}As and GaAs results in biaxial compression of the quantum well. The structures consist of a 250 nm-thick undoped GaAs buffer layer, carbon δ -layer, a 7 nm spacer of undoped GaAs, a 10 nm In_{0.2}Ga_{0.8}As well, a 7 nm spacer of undoped GaAs, a carbon δ -layer and 200 nm cap layer of undoped GaAs. The samples were mesa etched into standard Hall bars and then an Al gate electrode was deposited by thermal evaporation onto the cap layer through a mask. Varying the gate voltage V_g we were able to change the hole density p and mobility μ within the following ranges: $p = (2.5 \dots 8.0) \times 10^{11} \text{ cm}^{-2}$, $\mu = (1000 \dots 5700) \text{ cm}^2/\text{Vs}$. Two Hall bars prepared from each of the waffles 3856 and 3857 with close parameters were measured.

The magnetic field dependences of ρ_{xx} and ρ_{xy} at $T = 1.4 \text{ K}$ at different gate voltages for one of the samples investigated are presented in Fig. 1. It is clearly seen that despite the very large difference in conductivity values at $B = 0$, the magnetoresistance (MR) curves $\rho_{xx}(B)$ are very similar: the sharp negative MR at low magnetic field, which results from suppression of the interference contribution to the conductivity, is followed by the parabolic-like MR caused by the interaction correction.²³

Since our goal is to study the interaction correction let us briefly explain the method allowing us to extract it from the experimental data. Under our experimental conditions the parameter $T\tau$ is small enough ($T\tau < 0.1$) and therefore the main contribution comes from the diffusion part of the interaction correction. The unique property of the diffusion part is that it contributes to σ_{xx} but not to σ_{xy} . This fact opens a possibility to extract this correction reliably even when the correction value is small. The most straightforward way is to find such contribution to σ_{xx} which is absent in σ_{xy} . We extract these contributions by making use of the structure of the components of the conductivity tensor σ_{xx} and σ_{xy} . As shown in Ref. 24 the weak localization correction and the ballistic part of the interaction corrections are reduced to renormalization of the transport relaxation time and can be accounted for through the temperature and magnetic field dependence of the mobility. Thus σ_{xx} and σ_{xy} can be written as

$$\sigma_{xx}(B, T) = \frac{ep\mu(B, T)}{1 + \mu^2(B, T)B^2} + \delta\sigma_{xx}^{hh}(B, T), \quad (1)$$

$$\sigma_{xy}(B, T) = \frac{ep\mu^2(B, T)B}{1 + \mu^2(B, T)B^2}, \quad (2)$$

where $\delta\sigma_{xx}^{hh}(B, T)$ is the diffusion part of the interaction correction. If the Zeeman splitting is very small as compared with the temperature, $\delta\sigma_{xx}^{hh}$ is magnetic field inde-

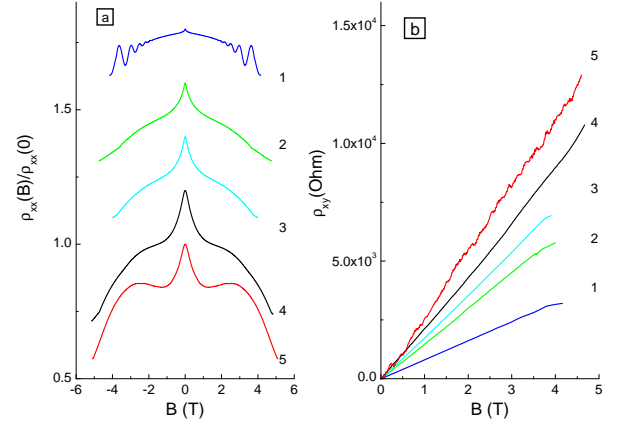


FIG. 1: The magnetic field dependences of ρ_{xx} (a) and ρ_{xy} (b) at $T = 1.4 \text{ K}$ for different gate voltages, which are characterized by the following values of p , σ_0 , and $\sigma(T = 1.4 \text{ K})$: $8 \times 10^{11} \text{ cm}^{-2}$, $59.6 G_0$, and $56.9 G_0$ (curves 1); $4.5 \times 10^{11} \text{ cm}^{-2}$, $9.9 G_0$, and $6.8 G_0$ (curves 2); $3.9 \times 10^{11} \text{ cm}^{-2}$, $8.1 G_0$, and $4.37 G_0$ (curves 3); $3 \times 10^{11} \text{ cm}^{-2}$, $3.9 G_0$, and $0.36 G_0$ (curves 4); $2.6 \times 10^{11} \text{ cm}^{-2}$, $3.5 G_0$, and $0.027 G_0$ (curves 5). Structure 3856. For clarity, the curves in the panel (a) are separated in vertical direction by the value of 0.2.

pendent. It has the form^{2,6,7,8}

$$\frac{\delta\sigma_{xx}^{hh}(T)}{G_0} = \alpha_i \left[1 + 3 \left(1 - \frac{\ln(1 + F_0^\sigma)}{F_0^\sigma} \right) \right] \ln T\tau, \quad (3)$$

where the first term in square brackets is the exchange or the Fock contribution while the second one is the Hartree contribution (the triplet channel). For the following, we enter here the prefactor α_i which was absent in Refs. 2, 6, 7, 8.

Thus, knowing the hole density p we can find $\mu(T, B)$ from experimental σ_{xy} vs B dependences [with the help of Eq. (2)] and then calculate the first term in Eq. (1). The difference between experimental value of σ_{xx} and this term should give the diffusion part of the h - h correction to the conductivity. This method allows us to find $\delta\sigma_{xx}^{hh}(B, T)$ for relatively low σ_0 , when the interference contribution to MR is not negligible up to the high magnetic field.

In what follows we demonstrate how this method works considering the results obtained for one of the samples, fabricated on the basis of structure 3857.

Let us start with the case of high Drude conductivity, $\sigma_0 \simeq 30 G_0$ (for the details of determination of σ_0 see Ref. 25). First for each temperature we have inverted the resistivity tensor whose components measured experimentally and found the conductivity tensor components σ_{xy} and σ_{xx} [solid curves in Figs. 2(a) and 2(b)]. Then, using the obtained σ_{xy} vs B dependences we have found $\mu(B)$ [shown in inset in Fig. 2(a)] and calculated the experimental value of the first term in Eq. (1). Finally, subtracting the latter term from the experimental value of σ_{xx} we obtain $\delta\sigma_{xx}$ [see Fig. 2(c)], which is identified with the diffusion part of the h - h correction $\delta\sigma_{xx}^{hh}(B, T)$.

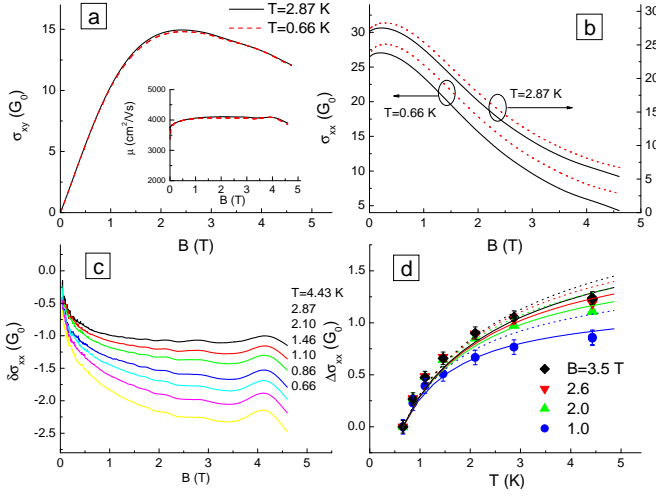


FIG. 2: (a) The experimental magnetic field dependences of σ_{xy} for two temperatures. The inset shows the magnetic field dependence of the mobility calculated from $\sigma_{xy}(B)$ for two temperatures with $p = 5.4 \times 10^{11}$ cm⁻². (b) The σ_{xx} vs B dependences for two temperatures. The solid curves are the data, the dotted curves are the first term of Eq. (1) calculated as described in text. (c) The magnetic field dependences of the difference between experimental and calculated σ_{xx} values for different temperatures. (d) The temperature dependences of $\Delta\sigma_{xx}$ at different magnetic fields. The symbols are the experimental results; curves are calculated dependences with $F_0^\sigma = -0.4$ (solid curves) and with $F_0^\sigma = -0.35$ (dotted curves). Structure 3857, $V_g = 2.4$ V, $\sigma_0 \simeq 30$ G₀.

As seen from Fig. 2(b) $\delta\sigma_{xx}$ is a small difference between two large quantities. That is why an accuracy in determination of $\delta\sigma_{xx}^{hh}(B, T)$, i.e., the absolute value of the interaction correction, is sufficiently low. In particular, it is very sensitive to the value of hole density, which is experimentally known with some accuracy. However, the difference of the quantities $\delta\sigma_{xx}$ taken at two temperatures for a given magnetic field (or taken at two magnetic fields for a given temperature) depends only slightly on the hole density and, therefore, is found with better accuracy.

In Fig. 2(d) we present the temperature dependences $\Delta\sigma_{xx}(T, B) = \delta\sigma_{xx}(T, B) - \delta\sigma_{xx}(T_0, B)$, where T_0 is the lowest temperature, obtained for different magnetic field. One can see that the higher is the magnetic field, the stronger is the change of $\Delta\sigma_{xx}$ with the temperature. This dependence can be attributed to the Zeeman splitting which leads to suppression of the triplet channel and, hence, to appearance of the magnetic field dependence of the interaction correction. Theoretically, the effect of Zeeman splitting has been considered in Refs. 8, 26, 27, and 6. However, the expressions derived there are too complicated and, therefore, inconvenient for the practical use. Much simpler expression, which well approximates

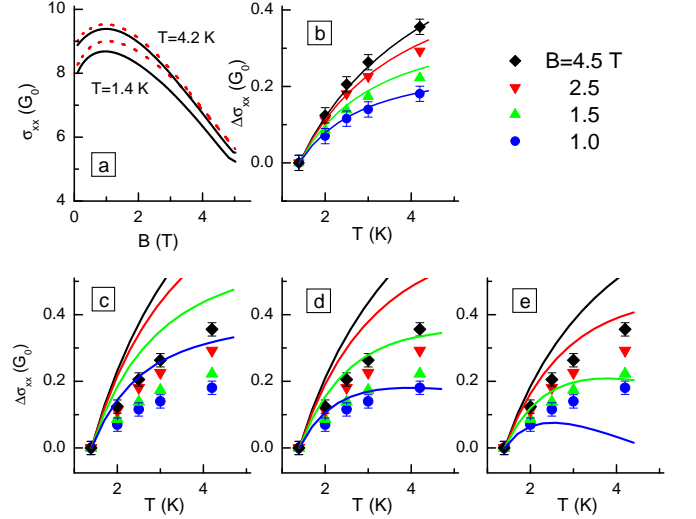


FIG. 3: (a) The magnetic field dependences of σ_{xx} for two temperatures. The solid curves are the data, the dotted curves are the first term of Eq. (1) calculated as described in text. (b) – (e) The temperature dependences of $\Delta\sigma_{xx}$ at different magnetic fields. The symbols are the experimental results; the curves are theoretical dependences calculated with: $\alpha_i = 0.5, F_0^\sigma = -0.43$ [panel (b)]; $\alpha_i = 1, F_0^\sigma = -0.45$ [panel (c)]; $\alpha_i = 1, F_0^\sigma = -0.5$ [panel (d)]; $\alpha_i = 1, F_0^\sigma = -0.55$ [panel (e)]. Structure 3857, $V_g = 2.8$ V, $p = 4.4 \times 10^{11}$ cm⁻², $\sigma_0 \simeq 11$ G₀.

these formulas, is^{22,28}

$$\frac{\delta\sigma_{xx}^{hh}}{G_0} = \alpha_i \left\{ \ln T\tau + \left[1 - \frac{\ln(1 + F_0^\sigma)}{F_0^\sigma} \right] \times \left[\ln T\tau + 2 \ln T\tau \sqrt{1 + \left(\frac{g\mu_B B}{T} \right)^2} \right] \right\}. \quad (4)$$

In Fig. 2(d) we plot the curves calculated according to Eq. (4) with $\alpha_i = 1, g = 3$,²⁹ and different F_0^σ values. One can see that the curves calculated with $F_0^\sigma = -0.4$ almost coincide with the experimental data.

Similar data treatment was carried out for the lower conductivity. In Fig. 3 we present the experimental and calculated magnetic field dependences of σ_{xx} [Fig. 3(a)] and $\Delta\sigma_{xx}$ -versus- T dependences for different magnetic fields [Fig. 3(b)] for $\sigma_0 = 11$ G₀ ($V_g = 2.8$ V). As seen from Figs. 3(c) – 3(e), it is impossible to describe the data by Eq. (4) with the prefactor $\alpha_i = 1$ for any F_0^σ -values. This is not surprising because the theory predicts $\alpha_i = 1$ only for large σ_0 value. However one can fit the data perfectly with $\alpha_i = 0.5$ and $F_0^\sigma = -0.43$ [see Fig. 3(b)].³⁰

To be sure that these changes in F_0^σ and α_i are not random we carried out systematical studies of the both structures at successive decrease of the hole density and Drude conductivity. It was recognized that Eq. (4) with the two fitting parameters, α_i and F_0^σ , describes well the experimental data down to $\sigma_0 \simeq 3.5 \pm 0.3$. All the results for α_i and F_0^σ are summarized in Fig. 4. The results of

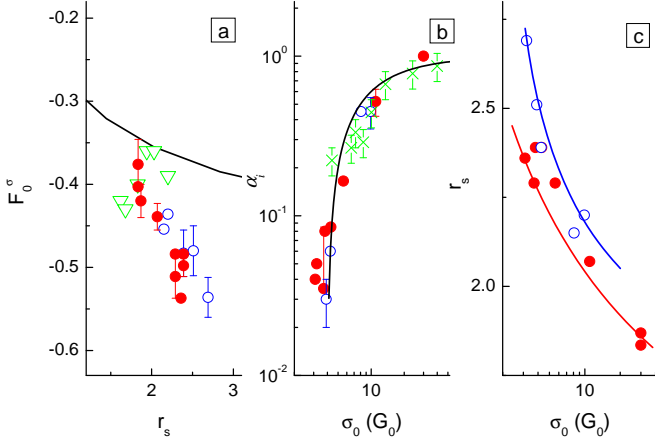


FIG. 4: (a) The r_s dependences of F_0^σ . (b) and (c) The σ_0 dependence of the prefactor α_i and the gas parameter r_s , respectively. Open and solid circles are the experimental data obtained in the present paper for structures 3856 and 3857, respectively. The triangles are data from Ref. 22. The crosses are the results of recalculation of the data obtained in Ref. 21. The curve in panel (a) is theoretical dependence, Eq. (6). The curve in panel (b) is the interpolating formula, Eq. (5). The curves in panel (c) are provided as a guide for the eye.

Ref. 22 for F_0^σ , obtained for $\sigma_0 > 30 G_0$ are presented in Fig. 4(a) also. One can see that all data match well. The scatter of the data from Ref. 22 is broader than that obtained here due to the large ballistic contribution that complicates the determination of F_0^σ . Note the α vs σ_0 data can be interpolated by the empirical formula

$$\alpha_i = 1 - \frac{4 G_0}{\sigma_0}. \quad (5)$$

Let us firstly discuss the behavior of the Fermi liquid parameter F_0^σ . Its value as a function of the gas parameter, r_s , is plotted in Fig. 4(a). It is seen that F_0^σ appreciably decreases with r_s that it becomes less than -0.454 at $r_s \simeq 2$. It is the value where the interaction correction in zeroth magnetic field changes sign [see Eqs. (3) and (4)]. However, the change of the sign of the interaction correction does not result in the metallic-like behavior of the total conductivity. This is because the insulating-like WL quantum correction dominates in our samples. Nevertheless, this fact manifests itself in our experiment. Since the triplet channel is suppressed with the B -increase, the magnetic field inverts the sign of $\delta\sigma_{xx}^{hh}$ again. So the magnetoresistance should be positive at low magnetic field and negative at high field. This fact graphically shows itself as the maximum in ρ_{xx} vs B dependence, which is evident for $\sigma_0 \simeq 3.5 G_0$ at $B \simeq 2.8$ T [see Fig. 1(a)].

In Fig. 4(a) we have plotted the theoretical r_s depen-

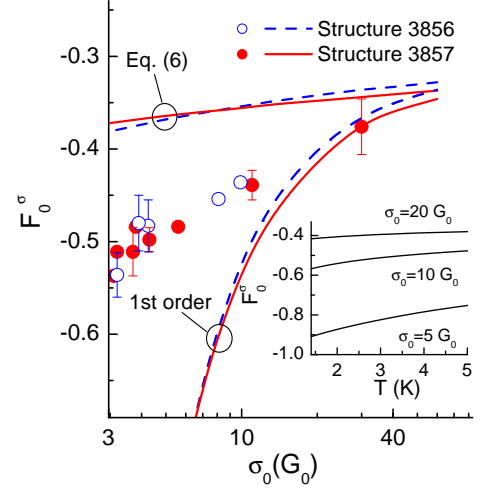


FIG. 5: (a) The σ_0 dependence of the interaction parameter F_0^σ . The symbols are the experimental data. The curves are theoretical dependences calculated as described in text.

dence of F_0^σ [Ref. 18]

$$F_0^\sigma = -\frac{1}{2\pi} \frac{r_s}{\sqrt{2-r_s^2}} \ln \left(\frac{\sqrt{2} + \sqrt{2-r_s^2}}{\sqrt{2} - \sqrt{2-r_s^2}} \right), \quad r_s^2 < 2$$

$$-\frac{1}{\pi} \frac{r_s}{\sqrt{r_s^2-2}} \arctan \sqrt{\frac{1}{2} r_s^2 - 1}, \quad r_s^2 > 2. \quad (6)$$

It is seen that experimental points strongly deviate downwards from the theoretical curve with increasing r_s . The possible reason of the deviation is the renormalization of the Fermi liquid constant F_0^σ with the decreasing Drude conductivity which strongly changes with r_s [see Fig. 4(c)]. This is directly evident from Fig. 5, where both the experimental and theoretical [Eq. (6)] F_0^σ vs σ_0 dependences are presented. When calculating the theoretical curves we have used the r_s vs σ_0 dependences from Fig. 4(c). It is seen that the lower the Drude conductivity the stronger the deviation.

Theoretically, the effect of renormalization of F_0^σ with the changing conductivity was studied in the framework of RG theory,^{3,6,7,8,16,17} which took the interaction into account in the first order in $1/\sigma$ exactly. According to this theory the temperature dependences of both σ and F_0^σ are the solutions of the system of differential equation

$$\frac{d\sigma}{d\xi} = - \left\{ 1 + 1 + 3 \left[1 - \frac{1+\gamma_2}{\gamma_2} \ln(1+\gamma_2) \right] \right\} \quad (7)$$

$$\frac{d\gamma_2}{d\xi} = \frac{1}{\sigma} \frac{(1+\gamma_2)^2}{2} \quad (8)$$

where $\xi = -\ln(T\tau)$, $\gamma_2 = -F_0^\sigma / (1 + F_0^\sigma)$, and σ is measured in units of G_0 . The term $1 + 1$ in braces is responsible for the weak localization and the interaction in singlet channel which in the case of Coulomb interaction give equal contributions.

The above system of differential equations have been solved numerically with the following initial conditions. We suppose that the high-temperature conductivity is equal to the Drude conductivity: $\sigma(\xi = 0) = \sigma_0$. The second condition is $\gamma_2(\xi = 0) = -F_0^\sigma / (1 + F_0^\sigma)$ where F_0^σ is determined by Eq. (6).³¹ Note this system describes the conductivity as a function of the parameter $T\tau$ (i.e., as a function of temperature). Experimentally, we are able to find the interaction contribution within only the relatively narrow temperature range, $T = 1.4 - 4.5$ K. Therefore it is more appropriate to compare the σ_0 dependence of F_0^σ rather than the temperature one. The solutions obtained for several σ_0 values, as the F_0^σ vs T dependence within the actual temperature range are presented in inset in Fig. 5. It is seen that this dependence is relatively weak. In order to compare these results with the experimental data for F_0^σ we have averaged the calculated value of F_0^σ over this temperature interval. Namely this averaged value is presented in Fig. 5 as a function of σ_0 .

It is seen that both the experimental and calculated values (labelled as “1st order”) of F_0^σ decrease with decreasing σ_0 . However, the theory gives much faster decrease. Most probably such a discrepancy indicates that one should take into account the next terms in $1/\sigma$ expansion in RG equations. To the best of our knowledge this has been done only for two particular cases inappropriate to our situation. The first case relates to multi-valley ($n_v \gg 1$) systems with $\gamma_2 \ll 1$.¹⁷ The second one is single valley ($n_v = 1$) systems but with the large γ_2 value.³²

Thus, realizing the crudity of the above estimations we, nevertheless, believe that the decrease of the experimental value of F_0^σ with the decreasing Drude conductivity results from the renormalization of the h - h interaction.

Strictly speaking, the RG equations (7) and (8) were derived in the absence of magnetic field, whereas the Zeeman splitting suppresses the triplet contributions to the right-hand side of Eqs. (7) and (8).^{6,8,26,27} Recently, it was shown that the effect of Zeeman splitting on conductivity can be used for extracting the dependence of F_0^σ on temperature.^{33,34,35} In our case the temperature range in which the Zeeman splitting is strong, $g\mu_B B > T$, is small fraction of the total interval which we use for averaging. Therefore, we do not expect significant difference in our results for F_0^σ due to taking into account the Zeeman

splitting and consider the comparison of our data with solutions of Eqs. (7) and (8) is almost correct.

Next we discuss the behavior of the prefactor α_i . Fig. 4(b) shows that α_i decreases sharply when σ_0 lowers. The behavior of the interaction correction with decreasing σ_0 was studied experimentally for the n -type 2D structures in Ref. 21. The recalculated data from this paper presented in Fig. 4(b) by crosses demonstrate analogous decrease also. The possible reason of such α_i vs σ_0 dependence is the interplay between the interference and the interaction which has not been taken into account in the RG theory.^{16,17} As shown in Refs. 36 and 37 two additional terms in the expression for the conductivity arise if this interplay is allowed for [see Eq. (40) in Ref. 37]. One term depends on the magnetic field and leads to appearance of the prefactor in WL magnetoresistance. The second one does not depend on the magnetic field, and therefore it was away in Ref. 37. It is quite possible that namely this term leads to decrease of α_i , prefactor in the interaction correction, with decreasing Drude conductivity. Another contribution to the prefactor α_i is due to the second-loop interaction effect. This correction is known for the singlet channel in the unitary ensemble (strong magnetic field).³⁸ To the best of our knowledge the impact of the interplay between the interaction and the interference upon the interaction correction to the conductivity as well as the second-loop contribution in the triplet channel for $n_v = 1$ is yet to be studied.

In summary, the behavior of the interaction contribution to the conductivity with decreasing Drude conductivity is determined both by the renormalization of the interaction constant F_0^σ and by the decrease of the prefactor α_i in Eq. (4), and the latter is more pronounced.

Acknowledgments

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